SS 2013 – Crystal bases and combinatorics

- Definition and motivation. What are quantum groups and why are they interesting? Literature: Hong-Kong, Introduction to quantum groups and crystal bases, Introduction + Chapter 3
- 2. Crystals bases for beginners, Chapter 4 Christian
- 3. Global bases, Chapter 6
- 4. Combinatorial model for crystals: Young tableaux, Chapter 7+8
- 5. Generalizing to symmetrizable Kac-Moody algebras: The path model Peter
- 6. Local properties of crystals, Literature: Stembridge "A local characterization of simply-laced crystals", Danilov-Karzanov-Koshevoy "B_2 crystals: axioms, structure, models"
- 7. Perfect crystals and what is it all about KR-modules Ghislain
- 8. Geometric realization of crystals: Nakajima's quiver varieties Bea
- 9. **Geometric realization of crystals: MV polytopes**, Literature: Kamnitzer "MV cycles and polytopes" *Jacintha*
- 10. Combinatorial models: Benchmark
- 11. Crystal bases for Super Lie algebras: What are the problems, what is proven?

The main guideline for the working group is a seminar at the MIT from spring 2011. (<u>http://math.mit.edu/~ptingley/QuantumGroupsSpring2011/</u>)

If you have any further suggestions for further talks or doubting that one of the talks above is useful, please let me know. Also, if you are interested in giving a talk, do not hesitate, **first come first serve**.

Best, Ghislain