Abstract: Fix a linear polynomial P(m) = dm + c with integer coefficients and consider the Simpson moduli space M of semistable sheaves with this Hilbert polynomial on the projective plane. A generic sheaf in M is a line bundle on its Fitting support, which is a planar projective curve of degree d.

For the infinite series of moduli spaces corresponding to the Hilbert polynomials dm - 1, d > 3, we study the geometry of the closed subvariety M' of sheaves that are not vector bundles on their support. M' is a singular variety of codimension 2 in M.

Our aim is to substitute M' in M by a divisor and interpret the result as a space of vector bundles on curves.