

Universität zu Köln Mathematisches Institut Prof. Dr. F. Vallentin Dr. A. Gundert A. Heimendahl

Methods and problems in discrete mathematics

Wintersemester 2019/20

— Exercise Sheet 1 —

**Exercise 1.1** Write the inverse power law  $f(r) = 1/r^s$ , for s > 0, as a nonnegative combination of functions  $r \mapsto (4-r)^k$ , with k = 0, 1, 2, ...

Exercise 1.2 Apply the spherical design strength test to

- (a) the vertices of the regular N-gon in the plane,
- (b) the vertices of the regular simplex in n dimensions,
- (c) the vertices of the regular cross polytope in n dimensions,
- (d) the  $E_8$  roots.

**Exercise 1.3** Compute the linear programming bound numerically for the following parameters and potential functions *f*:

- (a)  $n = 3, N = 20, f(r) = 1/r^{1/2},$
- (b)  $n = 10, N = 40, f(r) = (4 r)^k, k = 0, 1, 2, ..., 10.$

Software suggestion: https://www.sagemath.org/

**Exercise 1.4** Discuss how the linear programming bound can be generalized to the case of unequally charged particles.

"Hand-in": Until Thursday October 17, 10 am, using the form on the course homepage.