

# From Calculus to Cohomology

## Homework 9

**Exercise 1.** Let  $U$  and  $V$  be open subsets of a smooth manifold, such that  $U$ ,  $V$  and  $U \cap V$  have finite dimensional de Rham cohomology. Prove that

$$\chi(U \cup V) = \chi(U) + \chi(V) - \chi(U \cap V).$$

**Exercise 2.** Give an example of a Morse function on  $\mathbb{R}P^n$  and use it to find  $\chi(\mathbb{R}P^n)$  Hint: look at example 12.10.

**Exercise 3.** Exercises 12.1, 12.2, 12.5.

**Suggested Exercise 1.** Exercises 12.10, 12.7, 12.4.

These exercises are to be discussed on Tuesday January 16th.